## Math 32BH Homework 2 Solutions

I graded 4 of the problems: Page 270: 8, 10, 20, 24.

The following are solutions to the homework problems and additional comments for the problems I graded. Note that solutions are often brief; if you need more detail please ask in section or office hours. I may well have made errors in my solutions so please let me know if I did. For grading information see my class webpage.

## **General Comments**

The maximum number of points was 12. The high score was 12, the median was 12, and the mean was 11.5.

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- 3. Since  $\sin 3\theta$  is zero at  $\theta = 0$  and  $\theta = \pi/3$  and non-zero in between, we can evaluate  $\int_0^{\pi/3} \int_0^{2\sin 3\theta} r \, dr \, d\theta = 2 \int_0^{\pi/3} \sin^2 3\theta \, d\theta = \frac{\pi}{3}$ .
- 8. The circles intersect when  $\cos \theta = 3/4$ , so let  $\alpha = \cos^{-1} 3/4$ . Then the area is  $2 \int_{\alpha}^{\pi/2} \int_{0}^{4 \cos \theta} r \, dr \, d\theta + 2 \int_{0}^{\alpha} \int_{0}^{3} r \, dr \, d\theta = 4\pi + \alpha 4 \sin 2\alpha$ .

10.  $\int_0^{2\pi} \int_0^1 (4-r^2) r \, dr \, d\theta = \frac{7\pi}{2}.$ 

- 13. Solution is in the back of the book.
- 15. Solution is in the back of the book.

20. 
$$\int_{3\pi/2}^{2\pi} \int_{0}^{2\cos\theta} r^2 dr d\theta = \frac{16}{9}$$

24.  $\int_0^{2\pi} \int_2^4 (1 - 3\cos\theta\sin\theta) r^3 dr d\theta = 120\pi.$